



PID-controllers

Job van Amerongen

Control Engineering, Dept. of Electrical Engineering University of Twente, Netherlands www.ce.utwente.nl/amn J.vanAmerongen@utwente.nl

Contents

- Why PID-control
- When PID control
- Tuning rules (Ziegler-Nichols)
- Examples

- Most widely applied type of controller
 - in industry probably 90% of all controllers
- Available as single controllers or implemented in computers
- Applicable to many processes
- Give a reasonable performance
- Fuzzy is often PID-like as well



- Stopping a car at a traffic light
- Cruise control system

Controlling a car

- Stopping a car at a traffic light
- Goal
 - Stop in time at the white line



Variables



Cruise Control



I-action necessary in order to deal with constant disturbance at input of process

Proportional Control

- Limited accuracy for systems higher than first order
- Limited bandwidth



- For a second order system:
 PD-control ≈ state feedback
- Comparable with a lead network

PD-control is applicable as long as the system behaves more or less like a second-order system



- For increased accuracy of type-0 systems
 - add an integration
- Comparable with a lag network
- If dead time is dominant:
 - pure I-control



- For systems of type-0 and a dominant second-order behaviour
 - PID-control
- Can be seen as a combination of a lead and a lag network

Types of systems

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$$H(s) = \frac{K}{(s\tau_1 + 1)(s\tau_2 + 1)(s\tau_3 + 1)(...)}$$
PID typical S-curve

$$\mathcal{H}(s) = \frac{K e^{-sT_{d}}}{(s\tau_{1}+1)}$$





Border of instability

- After a few experiments we find
 - controller gain $K_u = 10$ brings the system at the border of instability
- A gain margin of 6 dB (a factor two) is a reasonable choice for the gain of a proportional controller

Response (GM = 6 dB)

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Nyquist plot



PI-controller (parallel)

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PI-controller (series)

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Ziegler-Nichols rules



Oscillation period

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PI-response



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PID-controller (series)

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with pole in origin

Ziegler-Nichols rules



PID-response



Disturbance rejection



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Tuning (τ and T_{d})



Border of instability

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P-controller



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PI-controller

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PID-controller



Tuning (τ and T_{d})



Border of instability

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PI-control



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Optimal tuning

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Optimal tuning



- PID-control suited for:
 - systems with an S-shaped response
 - systems with time delay
- Ziegler Nichols rules give 'reasonable' responses
 - (more suited for disturbance rejection than for tracking)
- Better tuning possible